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# LSPRAY—A Lagrangian Spray Solver User's Manual

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# LSPRAY - a Lagrangian Spray Solver - User's Manual

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## **Abstract**

LSPRAY is a Lagrangian spray solver developed for application with parallel computing and unstructured gas flow solvers. It is designed to be massively parallel and could easily be coupled with any existing gas-phase flow and/or Monte Carlo Probability Density Function (PDF) solvers. The solver accommodates the use of an unstructured mesh with mixed elements of either triangular, quadrilateral, and/or tetrahedral type for the gas flow grid representation. It is specifically used for fuel sprays within gas turbine combustors, but it has many other uses. The manual provides the user with the coding required to couple the spray code to any given flow code and a basic understanding of the LSPRAY code structure and the models involved in the spray formulation. The source code of LSPRAY will be available with the National Combustion Code (NCC) as a complete package.

## Table of Contents

I.	Nomenclature	4
II.	Introduction	6
III.	Governing Equations for the Gas Phase	8
IV.	Governing Equations for the Liquid Phase	9
V.	Details of Fuel Injection	11
VI.	Details of the Numerical Method	12
VII.	Program LSPRAY Flow Structure & Time-Averaging of the Interphase Source Terms of the Gas Phase Equations	15
VIII.	Parallelization	16
IX.	Details of the Coupling LSPRAY With the Flow & Monte Carlo PDF solvers	18
X.	Acknowledgements	21
XI.	References	22
APPENDICES		
I.	A List of LSPRAY Fortran subroutines and functions	25
II.	Description of LSPRAY Fortran subroutines and functions	27
III.	A Subroutine Listing for the Read Parameters of LSPRAY and EUPDF - an Eulerian PDF Solver	31
IV.	A Subroutine Listing for LSPRAY Code Initialization and Restart	35
V.	An Example LSPRAY Input file	53

VI.	A Subroutine Listing for LSPRAY and EUPDF Data Output	55
VII.	A Listing of Geometric Variables Used in LSPRAY and EUPDF	59
VIII.	An Example of the Partial Listings of Code Initiation for Coupling LSPRAY and EUPDF With a Gas Flow Solver	61
IX.	An Example Summary of CPU Times Taken By COR-SAIR and LSPRAY	65

## I. List of symbols

$\underline{a}_n$	outward area normal vector of the nth face
$B_k$	Spalding transfer number, defined in Eq. 19
$C_p$	specific heat, J/(Kg K)
$D$	turbulent diffusion coefficient, m <sup>2</sup> /s
$d$	droplet diameter, m
$dt$	time increment, s
$dt_{gl}$	global time step (liquid phase), s
$dt_{il}$	injection time step (liquid phase), s
$dt_{ml}$	allowable time step (liquid phase), s
$h$	specific enthalpy, J/Kg
$l_k$	latent heat of evaporation, J/Kg
$M_i$	molecular weight of ith species, kg/(kg-mole)
$m_k$	droplet vaporization rate, Kg/s
$n_k$	droplet number in kth group
$P$	pressure, N/m <sup>2</sup>
$P_n$	pressure at normal conditions, N/m <sup>2</sup>
$P_r$	Prandtl number
$R_u$	Gas constant, J/(Kg K)
$r$	radial coordinate (gas-phase equations) or droplet radius (liquid-phase equations), m
$S_c$	Schmidt number
$S_k$	droplet radius squared, $r_k^2$ , m <sup>2</sup>
$S_{ml}$	liquid inter-phase source term of gas-phase equations associated with $dt_{ml}$
$S_{mlc}$	liquid inter-phase source term of the gas-phase continuity equation
$S_{mle}$	liquid inter-phase source term of the gas-phase energy equation
$S_{mlm}$	liquid inter-phase source term of the gas-phase momentum equations
$S_{mls}$	liquid inter-phase source term of the gas-phase species equations
$T$	temperature, K
$t$	time, s
$U_k$	velocity component of kth droplet group, m/s
$u$	velocity component, m/s
$V_c$	volume of the computational cell, m <sup>3</sup>
$V_k$	velocity component of kth droplet group, m/s
$v$	velocity component, m/s
$W_k$	velocity component of kth droplet group, m/s
$w$	velocity component, m/s
$\dot{w}_j$	gas phase chemical reaction rate, 1/s
$x$	Cartesian coordinate
$Y$	gaseous species mass fraction

$y$  Cartesian/radial coordinate  
 $z$  Cartesian coordinate

#### greek symbols

$\Delta V$  computational cell volume,  $\text{m}^3$   
 $\delta$  Dirac-delta function  
 $\epsilon_j$  species mass fraction at the droplet surface  
 $\lambda$  thermal conductivity,  $\text{J}/(\text{m s K})$   
 $\mu$  dynamic viscosity,  $\text{kg}/(\text{m s})$   
 $\rho$  density,  $\text{kg}/(\text{m}^3)$   
 $\tau$  viscous stress term in Eq. 3,  $\text{kg}/(\text{m s}^2)$   
 $\chi$  mole fraction  
 $\sigma_l$  surface tension,  $\text{kg}/\text{s}^2$   
 $\theta$  void fraction

#### superscripts

$-$  time averaging  
 $//$  fluctuations

#### subscripts

$b$  represents conditions at boiling temperature  
 $c$  cell-face center  
 $f$  represents conditions associated with fuel  
 $g$  global or gas-phase  
 $k$  droplet group or liquid phase  
 $l$  liquid phase or laminar  
 $m$  conditions associated with  $dt_{ml}$   
 $n$  nth-face of the computational cell  
 $o$  initial conditions or oxidizer  
 $p$  grid cell or particle location  
 $s$  represents conditions at the droplet surface or adjacent computational cell  
 $i$  coordinate or specie indices  
 $j$  specie indices  
, partial differentiation with respect to the variable followed by it

## II. Introduction

There are many occurrences of sprays in a variety of industrial and power applications and materials processing. A liquid spray is a two phase flow with the gas as the continuous phase and the liquid as the dispersed phase in the form of droplets or ligaments.<sup>1</sup> The interaction between the two phases, which are coupled through exchanges of mass, momentum, and energy, can occur in different ways at disparate time and length scales involving various thermal, mass, and fluid dynamic factors.

A number of finite-difference formulations have been advanced over the years for predicting the flow (mass and momentum) and thermal properties of a rapidly vaporizing spray. Some of the pros and cons of various formulations can be found in Refs. 1 to 3. Depending on the nature of the spray, an appropriate selection could be made from the choice of multicontinua, discrete-particle, and probabilistic spray formulations, Lagrangian or Eulerian representation for the liquid-phase equations, and different vaporization models. In this manual, we only summarize the salient aspects of the spray formulation adopted from our previous work<sup>4-9</sup> without attempting to provide an in-depth review on the subject of the thermal theory and fluid dynamic behavior of reacting sprays.

LSPRAY employs the multicontinua approach, which allows for resolution on a scale greater than the average spacing between two neighboring droplets.<sup>1</sup> An Eulerian scheme is assumed for the gas phase equations and a Lagrangian scheme is used for the liquid phase equations as it eliminates errors associated with numerical diffusion. The vaporization model of a polydisperse spray takes into account the transient effects associated with the droplet internal heating and the forced convection effects associated with droplet internal circulation and the phenomena associated with boundary layers and wakes formed in the intermediate droplet Reynolds number range.<sup>5</sup> The present formulation is based on a deterministic particle tracking method and on a dilute spray approximation which is applicable for flows where the droplet loading is low. Not considered in the present release of the code are the effects associated with the droplet breakup, the droplet/shock interaction, the multi-component nature of liquid spray and the phenomena associated with dense spray effects and super-critical conditions. The numerical method used could be used in both unsteady and steady state calculations.<sup>6-9</sup>

The success of any numerical methodology used in the study of practical combustion flows depends not only on the modeling and numerical accuracy considerations, but its applicability would be dictated mainly by the available computer memory and turnaround times afforded by the present-day computers.



Our previous work on the extension of the Monte Carlo PDF approach to spray flames showed that the computer turnaround times and memory restrictions could be reduced considerably by exploiting the recent advances in parallel computer architectures.<sup>8</sup> It is well known that considerable effort usually goes into generating traditional structured grid meshes for gridding up practical combustor geometries which tend to be very complex in shape and configuration. The grid generation time could be reduced considerably by making use of existing automated unstructured grid generators.<sup>10</sup>

With the aim of advancing the current multi-dimensional computational tools used in the design of advanced technology combustors, we have recently extended our previous work on sprays to unstructured grids following the guidelines established for the development of the National Combustion Code (NCC).<sup>9</sup> NCC is being developed in the form of a collaborative effort between NASA LeRC, aircraft engine manufacturers, and several other government agencies and contractors.<sup>11</sup> Some of the salient features of our work in Ref. 9 are summarized below:

- (1) An efficient particle search algorithm was developed and implemented into the Lagrangian spray solver in order to facilitate particle movement in an unstructured grid of mixed elements.

- (2) The spray solver was designed to be massively parallel in order to exploit the recent advances in parallel architectures. The spray code was rewritten in Fortran 77 with PVM calls for parallel computing.

- (3) LSPRAY is currently coupled with Pratt and Whitney's CORSAIR<sup>12</sup> - an unstructured flow solver, and an Eulerian-based Monte Carlo probability density function solver - EUPDF,<sup>13</sup> which were selected to be integral components of the NCC cluster of modules. EUPDF was developed for application with sprays, combustion, unstructured grids and parallel computing.

- (4) The spray solver receives the mean velocity and turbulence fields from the flow solver. The species solution supplied could be provided by either a conventional CFD solver or a Monte Carlo PDF solver depending on the choice of the solver.

- (5) The spray solver computes the interphase source terms which are used by the gas phase solvers. This output could be used in both conservative as well as non-conservative finite-difference formulations of the gas phase equations.

The furnished code demonstrates the the successful methods used for coupling and parallelization of the spray to the flow code. These methods can be adopted for coupling other spray codes to Navier-Stokes solvers. Not all of the spray coding is furnished in this manual. The code that is generic to spray codes has been omitted. Only code that is unique to coupling is given. However, the first release of the generic code will be available along with NCC as a complete package.

The spray model provided several favorable results when applied to stratified-charge rotary combustion (Wankel) engines and several other confined as well as unconfined spray flames.<sup>6-9</sup>

### III. Governing Equations for the Gas Phase

Here, we summarize the conservation equations for the gas phase in Eulerian coordinates derived for the multicontinua approach.<sup>1</sup> This is done for the purpose of identifying the interphase source terms arising from the exchanges of mass, momentum, and energy with the liquid phase.

The conservation of the mass leads to:

$$[\bar{\rho}V_c]_{,t} + [\bar{\rho}V_c u_i]_{,x_i} = S_{mlc} = \sum_k n_k m_k \quad (1)$$

For the conservation of the species, we have:

$$[\bar{\rho}V_c Y_j]_{,t} + [\bar{\rho}V_c u_i Y_j]_{,x_i} - [\bar{\rho}V_c D Y_{j,x_i}]_{,x_i} - \bar{\rho}V_c \dot{w}_j = S_{mls} = \sum_k \epsilon_j n_k m_k \quad (2)$$

where

$$\sum_j \dot{w}_j = 0 \text{ and } \sum_j \epsilon_j = 1$$

For the momentum conservation, we have:

$$[\bar{\rho}V_c u_i]_{,t} + [\bar{\rho}V_c u_i u_j]_{,x_j} + [pV_c]_{,x_i} - [\theta V_c \tau_{ij}]_{,x_j} - [(1 - \theta)V_c \tau_{lij}]_{,x_j} = S_{mlm} = \sum_k n_k m_k u_{ki} - \sum_k \frac{4\pi}{3} \rho_k r_k^3 n_k u_{ki,t} \quad (3)$$

where  $\theta$  = the void fraction of the gas which is ratio of the equivalent volume of gas to a given volume of a gas and liquid mixture. For dilute sprays, the void fraction is assumed to be equal to one. The shear stress  $\tau_{ij}$  in Eq. 3 is given by:

$$\tau_{ij} = \mu[u_{i,x_j} + u_{j,x_i}] - \frac{2}{3}\delta_{ij}u_{i,x_i}$$

For the energy conservation, we have:

$$[\bar{\rho}V_c h]_{,t} + [\bar{\rho}V_c u_i h]_{,x_i} - [\theta V_c \lambda T_{,x_i}]_{,x_i} - [(1 - \theta)V_c \lambda_l T_{,x_i}]_{,x_i} - [\theta V_c p]_{,t} = S_{mle} = \sum_k n_k m_k (h_s - l_{k,eff}) \quad (4)$$

#### IV. Governing Equations for the Liquid Phase

The equations of motion for each class of droplets are:

$$\frac{dx_k}{dt} = U_k \quad (5)$$

$$\frac{dy_k}{dt} = V_k \quad (6)$$

$$\frac{dz_k}{dt} = W_k \quad (7)$$

The above equations are for droplet position. For droplet velocity, we have:

$$\frac{dU_k}{dt} = \frac{3}{16} \frac{C_D \mu_{gs} Re_k}{\rho_k r_k^2} [U_g - U_k] \quad (8)$$

$$\frac{dV_k}{dt} = \frac{3}{16} \frac{C_D \mu_{gs} Re_k}{\rho_k r_k^2} [V_g - V_k] \quad (9)$$

$$\frac{dW_k}{dt} = \frac{3}{16} \frac{C_D \mu_{gs} Re_k}{\rho_k r_k^2} [W_g - W_k] \quad (10)$$

where

$$Re_k = 2 \frac{r_k \rho_g}{\mu_{gs}} \left[ (U_g - U_k)^2 + (V_g - V_k)^2 + (W_g - W_k)^2 \right]^{1/2} \quad (11)$$

$$C_D = \frac{24}{Re_k} \left( 1 + \frac{Re_k^{2/3}}{6} \right) \quad (12)$$

For droplet size, the droplet regression rate is determined from three different correlations depending upon the droplet-Reynolds-number range. When  $Re_k > 20$ , the regression rate is determined based on a gas-phase boundary-layer analysis<sup>14</sup> valid for Reynolds numbers in the intermediate range. The other two correlations valid when  $Re_k \leq 20$  are taken from Clift et al.<sup>15</sup>

$$\begin{aligned} \frac{dS_k}{dt} &= -2 \frac{\mu_l}{\rho_k} \left[ \frac{2}{\pi} Re_k \right]^{1/2} f(B_k) \quad \text{if } Re_k > 20 \\ \frac{dS_k}{dt} &= -\frac{\mu_l}{\rho_k} \left[ 1 + (1 + Re_k)^{1/3} \right] Re_k^{0.077} \ln(1 + B_k) \\ &\quad \text{if } 1 < Re_k \leq 20 \end{aligned} \quad (13)$$

$$\frac{dS_k}{dt} = -\frac{\mu_l}{\rho_k} \left[ 1 + (1 + Re_k)^{1/3} \right] \ln(1 + B_k) \quad \text{if } Re_k < 1$$

where  $B_k$  is the Spalding transfer number defined in Eq. 19. The function  $f(B_k)$  is obtained from the solution of Emmon's problem. The range of

validity of this function was extended in Raju and Sirignano<sup>4</sup> to consider the effects of droplet condensation.

The internal droplet temperature is determined based on a vortex model.<sup>14</sup> The governing equation for the internal droplet temperature is given by:

$$\frac{\partial T_k}{\partial t} = 17 \frac{\lambda_l}{C_{pl}\rho_l r_k^2} \left[ \alpha \frac{\partial^2 T_k}{\partial \alpha^2} + (1 + C(t)\alpha) \frac{\partial T_k}{\partial \alpha} \right] \quad (14)$$

where

$$C(t) = \frac{3}{17} \left[ \frac{C_{pl}\rho_l}{\lambda_l} \right] r_k \frac{dr_k}{dt} \quad (15)$$

where  $\alpha$  represents the coordinate normal to the streamsurface of a Hill's Vortex in the circulating fluid and  $C(t)$  represents a nondimensional form of the droplet regression rate. The initial and boundary conditions for Eq. 14 are given by

$$t = t_{injection}, \quad T_k = T_{k,o} \quad (16)$$

$$\alpha = 0, \quad \frac{\partial T_k}{\partial \alpha} = \frac{1}{17} \left[ \frac{C_{pl}\rho_l}{\lambda_l} \right] r_k^2 \frac{\partial T_k}{\partial t} \quad (17)$$

$$\alpha = 1, \quad \frac{\partial T_k}{\partial \alpha} = -\frac{3}{32} \frac{\rho_k}{\lambda_l} \left[ \frac{C_p(T_g - T_{ks})}{B_k} - l_k \right] \frac{dS_k}{dt} \quad (18)$$

where  $\alpha = 0$  refers to the vortex center and  $\alpha = 1$  refers to the droplet surface.

The Spalding transfer number is given by

$$B_k = \frac{C_p(T_g - T_{ks})}{l_{k,eff}} = \frac{(y_{fs} - y_f)}{(1 - y_{fs})} \quad (19)$$

$$l_{k,eff} = l_k + 4\pi \frac{\lambda_l r_k^2}{m_k} \left( \frac{\partial T_k}{\partial r} \right)_s \quad (20)$$

$$y_{fs}^{-1} = 1 + \frac{M_a}{M_f} (\chi_{fs}^{-1} - 1) \quad (21)$$

where  $l_{k,eff}$  is the effective latent heat of vaporization as modified by the heat loss to the droplet interior, and  $M_a$  is the molecular weight of the gas excluding fuel vapor.

Based on the assumption that phase equilibrium exists at the droplet surface, the Clausius-Clapeyron relationship yields

$$\chi_{fs} = \frac{P_n}{P} \exp \left[ \frac{l_k}{R_u} \left( \frac{1}{T_b} - \frac{1}{T_{ks}} \right) \right] \quad (22)$$

In Eq. 11 the molecular viscosity is evaluated at a reference temperature using Sutherland's equation

$$\mu(T_{ref}) = 1.4637 \cdot 10^{-6} \frac{T_{ref}^{3/2}}{T_{ref} + 120} \quad (23)$$

where

$$T_{ref} = \frac{1}{3}T_g + \frac{2}{3}T_{ks} \quad (24)$$

The droplets may evaporate, move along the wall surfaces, and/or reflect with reduced momentum upon droplet impingement with the combustor walls. In our present computations, subsequent to the droplet impingement with the walls, the droplets are assumed to flow along the wall surfaces with a velocity equal to that of the surrounding gas.

## V. Details of Fuel Injection

The success of any spray model depends a great deal on the specification of the appropriate injector exit conditions. However, a discussion involving the physics of liquid atomization is beyond the scope of this manual. In the present release of the code, the liquid fuel injection is simulated by introducing a discretized parcel of liquid mass in the form of spherical droplets at the beginning of every fuel-injection time step.

For certain cases, the fuel-injection time step,  $dt_{il}$ , needs to be determined based on the resolution permitted by the length and time scales associated with several governing parameters such as average grid spacing and average droplet spacing and velocity. However, for the case of a steady state solution, our experience showed that a time step based on the average droplet lifetime yields better convergence,<sup>4-7</sup> whose value typically ranges between 1 to 2 milli-seconds for the case of reacting flows.

The program facilitates fuel injection through the use of a single fuel injector comprising of different holes.<sup>6-7</sup> However, multiple fuel injection in a steady state calculation could be simulated by simply assigning different initial conditions for the spatial locations of the droplet groups associated with each one of the different holes. For a polydisperse spray, the program expects inputs for the number of droplet groups in a given stream and for the initial droplet locations and velocities. However, the number of droplets in a given group and their sizes could be either input directly or computed from a properly chosen function for the droplet size distribution. The specified initial inputs should be representative of the integrated averages of the experimental conditions.<sup>8-9</sup>

One correlation typical of those used for the droplet size distribution is taken from Ref. 16:

$$\frac{dn}{n} = 4.21 \cdot 10^6 \left[ \frac{d}{d_{32}} \right]^{3.5} e^{-16.98 \left( \frac{d}{d_{32}} \right)^{0.4}} \frac{dd}{d_{32}} \quad (25)$$

where  $n$  is the total number of droplets and  $dn$  is the number of droplets in the size range between  $d$  and  $d + dd$ . The Sauter mean diameter,  $d_{32}$ , could be either specified or estimated from the following correlation<sup>17</sup>:

$$d_{32} = B_d \frac{2\pi\sigma_l}{\rho_g V_T^2} \lambda_m^* \quad (26)$$

where  $B_d$  is a constant,  $V_T$  is the average relative velocity between the liquid interface and the ambient gas, and  $\lambda_m^*$  is a function of the Taylor number,  $(\rho_l \sigma_l^2)/(\rho_g \mu_l^2 V_T^2)$ .

LSPRAY contains a subroutine, **dropdis**, for the integration of a droplet size distribution function which could easily be modified for other correlations of similar kind. The droplet size distribution obtained from the above correlation in terms of the cumulative percentage of droplet number and mass as a function of the droplet diameter is shown in Fig. 1.

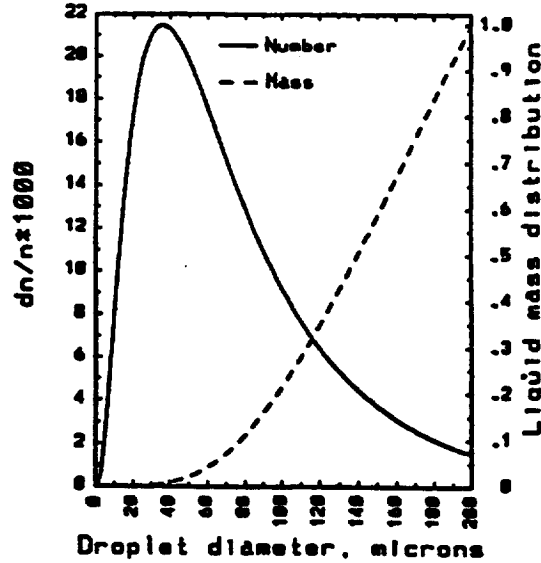


Figure 1. Droplet-size distribution.

## VI. Details of the Numerical Method

In order to evaluate the initial conditions for the integration of the liquid phase equations, we need to know the gas phase properties at each particle location. But in order to evaluate the gas phase properties it is first necessary to identify the computational cell where a particle is located. It is a

trivial task to search for the computational cell of the particle location in rectangular coordinates. However, a search for the particle location becomes a complicated problem when the computational cell is no longer rectangular in the physical domain. An efficient particle search algorithm is developed and implemented into the Lagrangian spray solver in order to facilitate particle movement in an unstructured grid of mixed elements. The search is initiated in the form of a local search from the computational cell of the previous time-step as the starting point. The location of the computational cell is determined by evaluating the dot product of  $\underline{x}_{pc} \cdot \underline{a}_n = |\underline{x}_{pc}| |\underline{a}_n| \cos(\phi)$ , where  $\underline{x}_{pc}$  is the vector defined by the particle location to the center of the n-face of the computational cell and  $\underline{a}_n$  is the outward area normal of the n-face as shown in Fig. 2, and  $\phi$  is the angle between the two vectors.

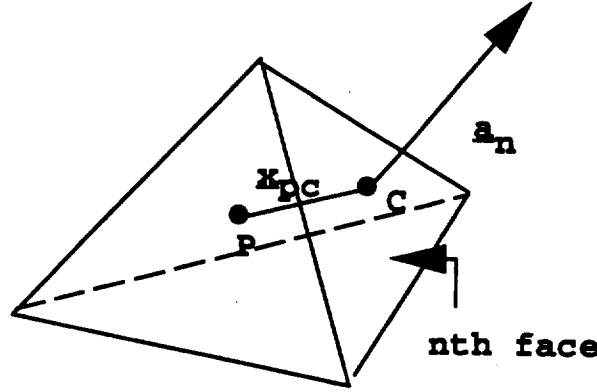


Figure 2. A vector illustration used in the particle search analysis.

A simple test for the particle location requires that the dot product be negative over each and every one of the n-faces of the computational cell. If the test fails, the particle search is carried on over to the adjacent cells of those faces over which the dot product turns out to be positive. Some of those n-faces might represent the boundaries of the computational domain while the others are the interfaces between two adjoining interior cells. The search is first carried on over to the adjacent interior cells in the direction pointed out by the positive sign of the dot products. The boundary conditions are implemented only after making sure that all the possibilities lead to a search outside of the computational boundaries. This implementation ensures against any inadvertent application of the boundary conditions before locating the correct interior cell.

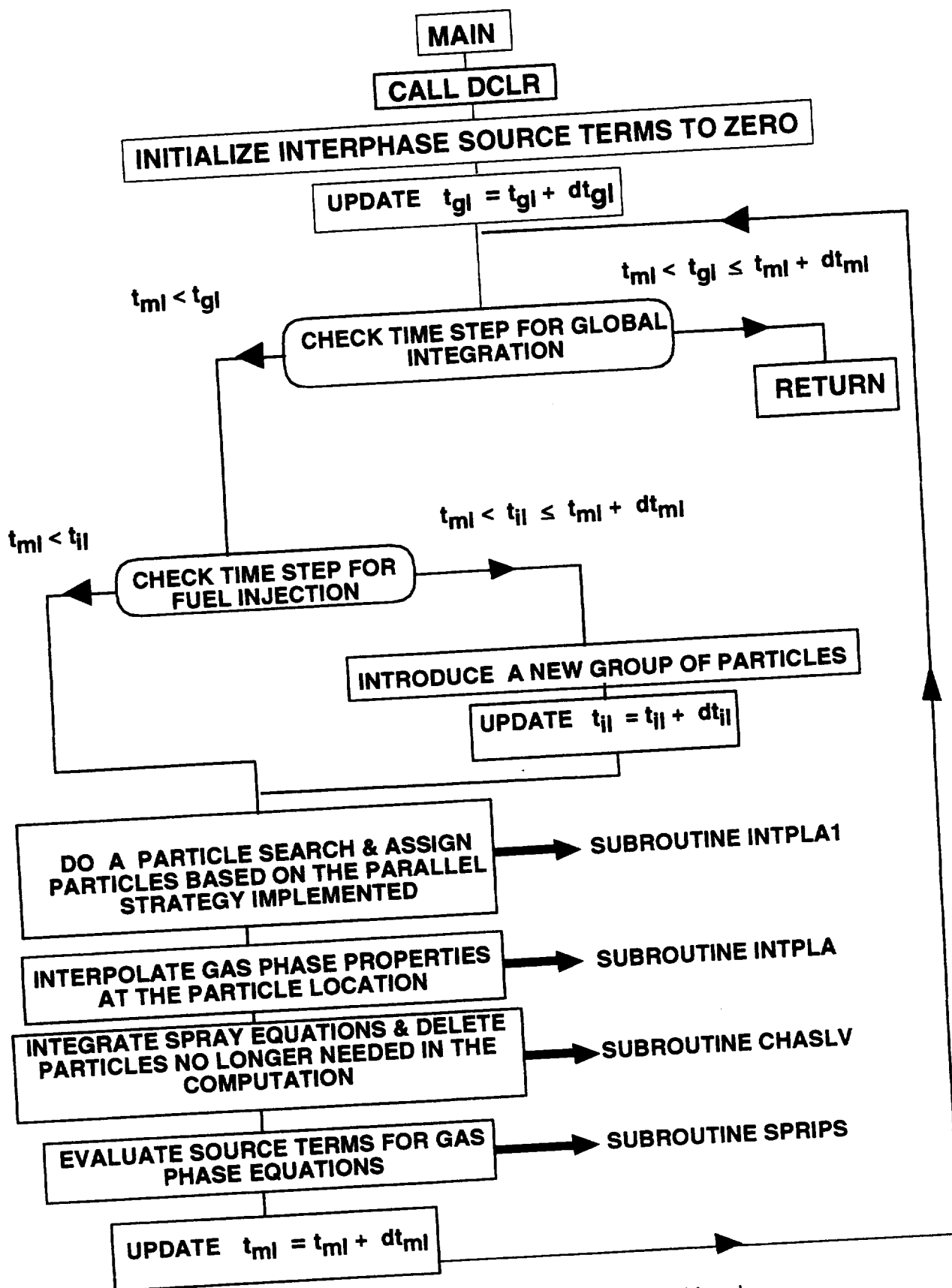


Fig. 3 The flow structure of the LSPRAY code.



After the gas phase properties at the particle location are known, the ordinary differential equations of particle position, size, and velocity are advanced by a second-order accurate Runge-Kutta method. The partial differential equations governing the droplet internal temperature distribution are integrated by an Euler method. After the liquid phase equations are solved, the interface source terms of the gas phase equations are evaluated.

## VII. Program LSPRAY Flow Structure & Time-Averaging of the Interphase Source Terms of the Gas Phase Equations

The spray solver makes use of three different time steps -  $dt_{ml}$  is the allowable time step,  $dt_{gl}$  is the global time step, and  $dt_{il}$  is the fuel injection time step.  $dt_{ml}$  needs to be evaluated based on the smallest of the different time scales, which are associated with various rate controlling phenomena of a rapidly vaporizing droplet, such as those imposed by an average droplet lifetime, the local grid spacing and a relaxation time scale associated with droplet velocity among others. This restriction usually leads to a small time-step which typically has values in the neighborhood of 0.01 milli-seconds (ms). However, our experience has shown that the convergence for the steady state computations could be improved greatly by supplying the flow and EUPDF solvers with the interphase terms obtained from a time-averaging procedure, where the averaging is performed over an average lifetime of the droplets,  $dt_{gl}$ . The variable,  $dt_{gl}$ , has values in the neighborhood of 1 ms.

The averaging scheme could be explained better through the use of a flow chart shown in Fig. 3. The main spray solver is invoked by a call to **dclr** which executes the following steps:

1. It first initializes the source terms to zero.
2. Checks to see if new particles need to be introduced.
3. Advances liquid phase equations over a pre-specified time step,  $dt_{ml}$ , with calls to the following routines:
  - intpla1** - Does a particle search and assigns particles based on the parallel strategy implemented.
  - intpla** - Interpolates gas phase properties at the particle location.
  - chaslv** - Advances liquid phase equations and, also, deletes any particles that are no longer needed in the computations.
  - sprips** - Evaluates the liquid phase source term contributions,  $S_{ml}$ , for use in the gas phase equations.

4. Continues with steps (2) and (3) until the computations are completed over a global time step of  $dt_{gl}$ .
5. Returns control over to other solvers, e.g. flow or EUPDF, and supply them with source terms,  $S_{gl}$ , averaged over  $dt_{gl}$ .

The time-averaged contribution of these source terms,  $S_{gl}$ , is given by:

$$S_{gl} = \sum_{m=1}^M \frac{dt_{ml}}{dt_{gl}} S_{ml} \quad (27)$$

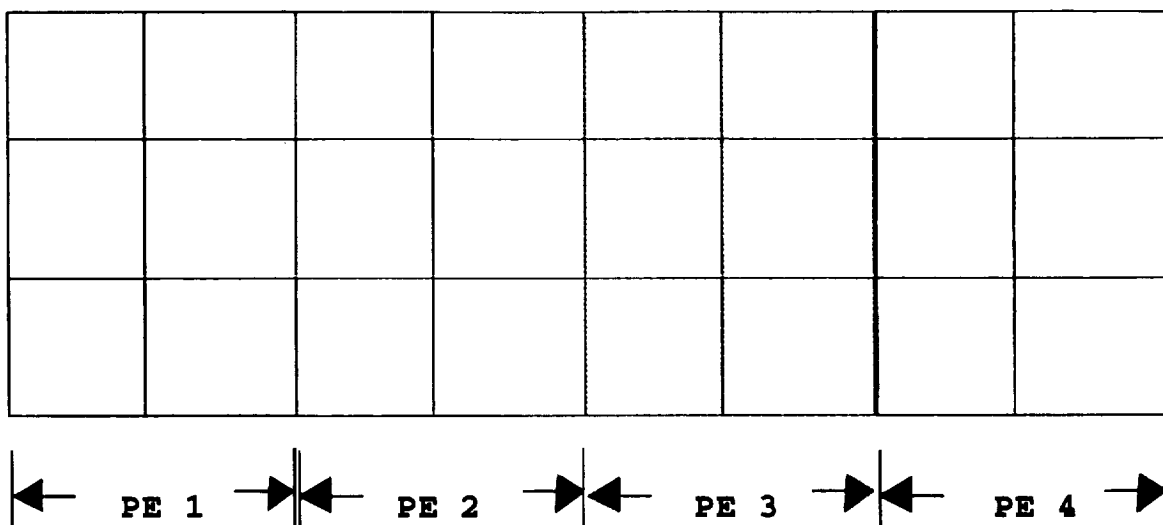
where

$$\sum_{m=1}^M dt_{ml} = dt_{gl} \quad (28)$$

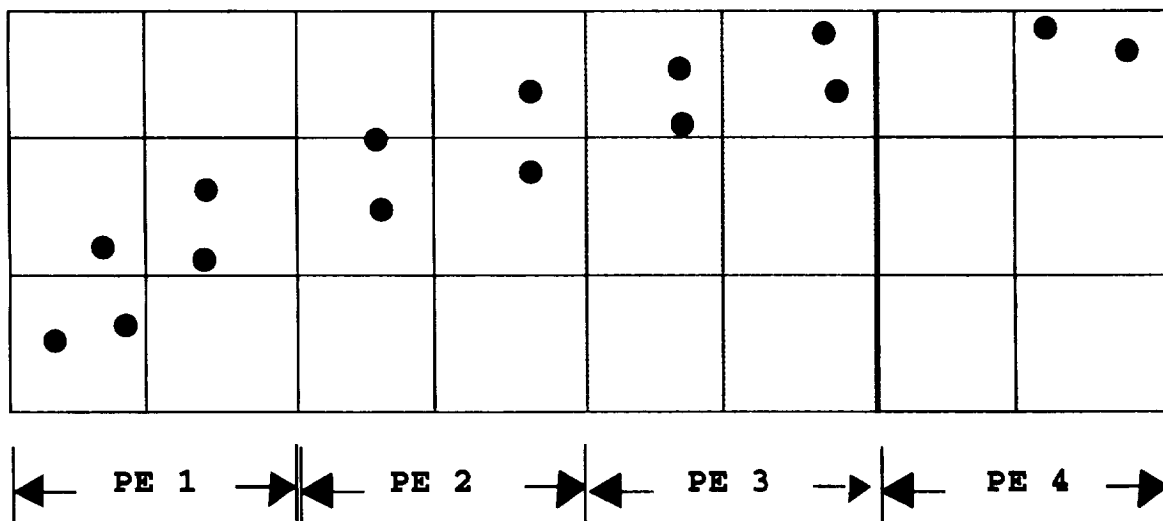
## VIII. Parallelization

There are several issues associated with the parallelization of the spray computations. The goal of the parallel implementation is to extract maximum parallelism so as to minimize the execution time for a given application on a specified number of processors.<sup>18</sup> Several types of overhead costs are associated with parallel implementation which include data dependency, communication, load imbalance, arithmetic, and memory overheads. The term arithmetic overhead is the extra arithmetic operations required by the parallel implementation. Memory overhead refers to the extra memory needed. Excessive memory overhead reduces the size of a problem that can be run on a given system and the other overheads result in performance degradation.<sup>18</sup> Any given application usually consists of several different phases that must be performed in certain sequential order. The degree of parallelism and data dependencies associated with each of the subtasks can vary widely.<sup>18</sup> The goal is to achieve maximum efficiency with a reasonable programming effort.<sup>18</sup>

In our earlier work, we discussed the parallel implementation of a spray algorithm developed for the structured grid calculations on a Cray T3D.<sup>8</sup> These computations were performed in conjunction with the extension of a Monte Carlo PDF method to spray flames. The parallel algorithm made use of the shared memory constructs exclusive to Cray MPP (Massively Parallel Processing) Fortran and the computations showed a reasonable degree of parallel performance when they were performed on a NASA LeRC Cray T3D with the number of processors ranging between 8 to 32.<sup>8</sup> Later on,



**Fig. 4a** An illustration of the parallelization strategy employed in the gas flow computations.



**Fig. 4b** An illustration of the parallelization strategy employed in the spray computations.

the extension of this method to unstructured grids and parallel computing in Fortran 77 with PVM calls was reported in Ref. 9. The Fortran 77 version offers greater computer platform independence. In this section, we only highlight some important aspects of parallelization.

In an approach, where an Eulerian scheme is employed for the gas phase computations and a Lagrangian scheme for the liquid phase computations, the gas phase computations are performed by simply dividing the domain of computation into  $n$ -parts of equal size and each part is solved by a different processor. Fig. 4a illustrates a simple example of the domain decomposition strategy adopted for the gas-phase computations where the total domain is simply divided equally amongst the available computer processing elements (PEs). In this case, we assumed the number of available PEs to be equal to four. But the Lagrangian representation makes the spray computations difficult to parallelize as spray distribution tends to be spatially very non-uniform and, also, dynamic in nature for the reasons summarized below:

(1) Most of the spray is usually confined to a small region near the atomizer location.

(2) The Lagrangian particles tend to move in and out of different parts of the computational domain processed by different PEs,

(3) Some new particles might be added to the computation at the time of fuel injection while some others might be taken out of computation either when they exit out of the computational boundaries or when they become too small after vaporization.

In order to evaluate the parallel performance of the spray computations, two different domain decomposition strategies were developed.<sup>9</sup> However, the present release of the code contains the one which showed better performance when the computations were performed on the LACE cluster of workstations at NASA LeRC.<sup>9</sup>

Fig. 4b illustrates a simple example of the domain decomposition strategy adopted for the liquid-phase computations where the corresponding gas-flow computational domain is divided into equal parts between the four available PEs. In this strategy, the Lagrangian particles are assigned to the processor of the computational grid where a particle is located. This strategy may lead to non-uniform load balancing during the integration of the liquid phase equations but is likely to result in less message passing since the inter-processor communications are limited to a single operation associated with the particle search.

## IX. Details of the Coupling LSPRAY With the Flow & Monte Carlo PDF Solvers

The spray module is designed so that it could easily be coupled with any of the existing unstructured-grid flow and Monte-Carlo-PDF solvers. If geo-

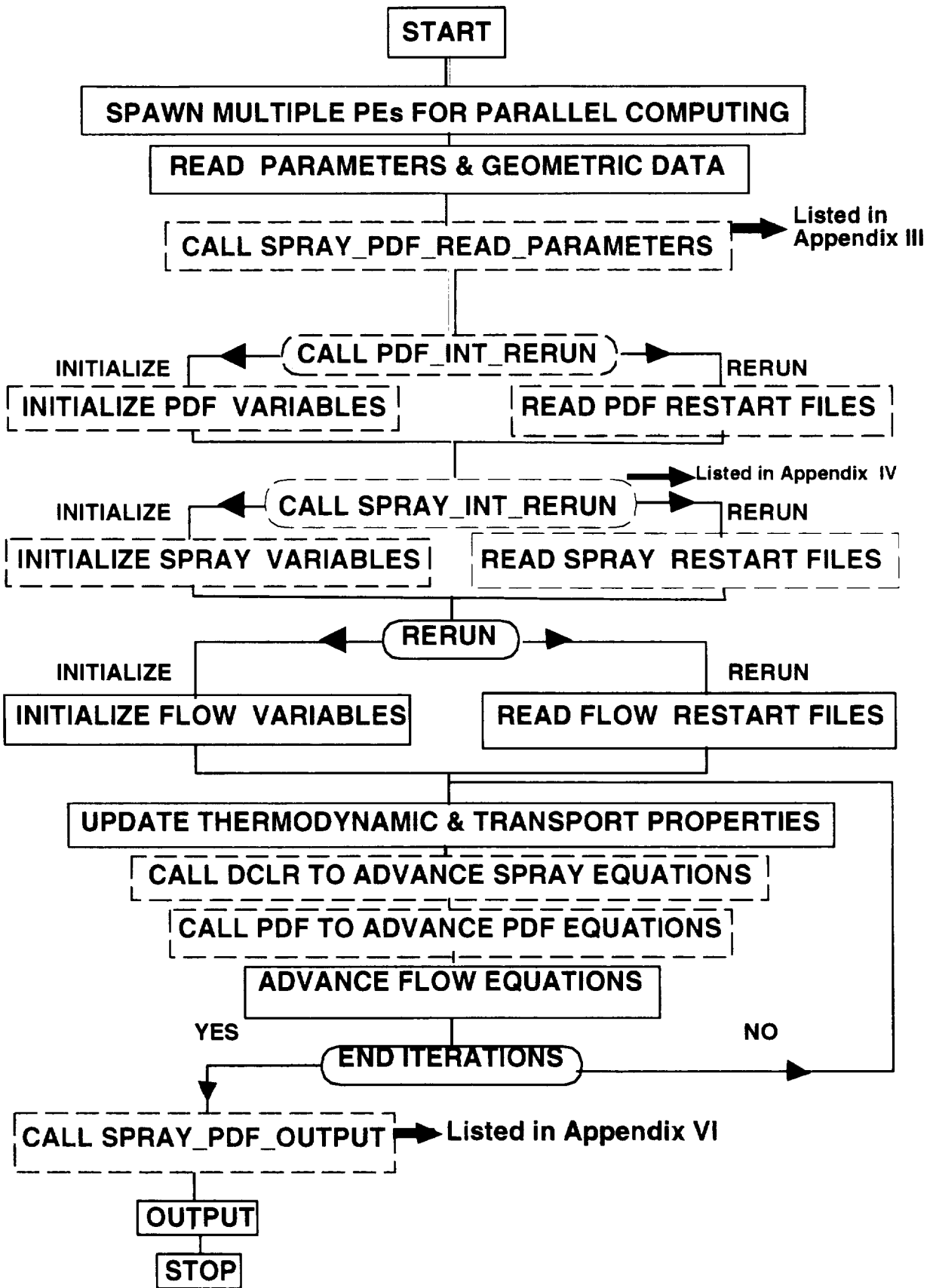


Fig. 5 The overall flow structure of the combined flow, LSPRAY, and EUPDF solvers.

metric grid parameters - e.g. area vectors, grid connectivity, etc., were supplied separately, it could even be coupled with any of the existing structured-grid flow solvers. However, the present release of the code relies on the other modules of NCC for obtaining that information.

The structure of the spray solver is so designed that only a minimal amount of coding modifications need to be made within the flow and PDF solvers for their coupling with LSPRAY. The present version of the module relies entirely on the use of the Fortran common blocks for information exchange between the various modules. Even this reliance should entail only few changes to be made within the spray code for linkage with different solvers.

The coupling issues could be understood better through the use of a flow chart shown in Fig. 5. The chart contains several blocks - some shown in black and/or solid lines and others in color and/or dashed lines. The ones in solid blocks represent the flow chart that is typical of most flow solvers. The ones in dashed blocks represent the coupling for adding the spray and PDF solvers. The details on the PDF blocks are not provided in this report as they could be found elsewhere in a separate reference.<sup>13</sup> It should be borne in mind that the PDF solver could be run without the spray solver and vice-versa as they are independent.

The flow chart for a typical flow solver begins by calling several routines - some for initiating the established PVM protocol for parallel computing and the others for spawning children of the same processes so that the computations could be performed simultaneously on various PEs participating in the parallel computing environment. It is followed by a routine to read various initial parameters. The geometric data could be either read directly or created by the inclusion of appropriate calling routines needed for grid generation. Then, the initial conditions for the flow variables need to be either specified or read from the restart files if it is a rerun. The thermodynamic and transport properties are then updated before advancing the flow equations over a series of time steps until the desired number of iterations are reached. Finally, the program is terminated after writing the output data on a separate restart and standard files.

The coupling starts with the addition of a calling routine - **spray\_pdf\_read\_parameters** - to read the spray and pdf control parameters followed by calls to the restart or initialization routines: **pdf\_int\_rerun** followed by **spray\_int\_rerun**. Then, calls to **dclr** and **pdf** were made in order to advance the spray and pdf equations in a sequential order before advancing the flow equations. It should be borne in mind that if the pdf solver is invoked, the thermodynamic and transport properties would be evaluated by the routines contained within the pdf solver instead of the ones contained in the flow solver. Also, Eqs. 1 to 4 - the gas phase governing equations

- need to be modified with the addition of the interphase source terms defined in Section III. Finally, a routine, `spray_pdf_output`, is included for outputting the pdf and spray data on appropriate restart and standard files.

Appendix I contains a table of all the Fortran subroutines and functions used in LSPRAY as well as the interface subroutines needed for coupling LSPRAY with a flow solver. All these routines will be released along with NCC but, however, a complete listing of all the interface subroutines is also provided in the user's manual. A brief description of all the LSPRAY routines is contained in Appendix II of the user's manual. The description pages of the LSPRAY routines along with the code listing pages of the interface routines are also given in this table.

Appendix III contains the listing of a subroutine which is used for reading some of the control and other associated parameters involving LSPRAY and EUPDF solvers. The LSPRAY initialization and restart routine is listed in Appendix IV. This routine provides a detailed account of all the input files associated with LSPRAY and gives a detailed description of how to initialize the code for the case of a swirl-stabilized confined spray flame. A sample input file is listed in Appendix V. This input applies for n-heptane fuel.

Appendix VI contains the listing of a subroutine used for writing output data from LSPRAY and EUPDF codes on separate standard and restart files.

Appendix VII contains a list of the geometric variables used by LSPRAY which are currently supplied by the flow code of NCC.

Appendix VIII contains an example of the partial listings of code initiation for coupling LSPRAY and EUPDF with a gas flow solver.

The last appendix provides an example of the summary of the CPU times taken by CORSAIR and LSPRAY for the case of a confined swirl-stabilized spray flame when the computations were performed on a LACE cluster at NASA LeRC.

## **X. Acknowledgements**

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## XI. References

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## Appendix I

Table 1. A List of LSPRAY Fortran subroutines and functions.			
Number	Name of the routine	Code released with NCC/Description page	Code page/ User's manual
1.	<i>blasiu()</i>	25	
2.	<i>chaslv</i>	25	
3.	<i>dclr</i>	25	
4.	<i>dropdis()</i>	26	
5.	<i>find_cntr()</i>	26	
6.	<i>find_xyz face()</i>	26	
7.	<i>intpla</i>	26	
8.	<i>intpla1</i>	27	
9.	<i>prnspr</i>	27	
10.	<i>spray_int_rerun</i>	27	31
11.	<i>spray_pdf_output</i>	27	49
12.	<i>spray_pdf_read_parameters</i>	27	28
13.	<i>sprips</i>	27	
14.	<i>sy()</i>	27	



## Appendix II

### Description of LSPRAY Fortran subroutines and functions

#### 1. function blaslu(x):

PURPOSE: This function returns a solution based on the Blasius function used in computing the mass, momentum, and heat transfer at the droplet surface.

#### 2. subroutine chaslv:

PURPOSE: This routine has the following functions:

- (1) Integrates the liquid phase equations.
- (2) Takes particles out of computation after becoming small enough due to vaporization.

#### 3. subroutine dclr:

PURPOSE: This routine is to be called once at the beginning every global time-step, dtgl. It is primarily a controlling routine for spray computations.

This routine has the following functions:

- (1) It initializes the source terms to zero.
- (2) Checks to see if new particles need to be introduced.
- (3) Advances liquid phase equations over an allowable or pre-specified time step, dtml, with calls to the following routines:

intpla1 - Interpolates gas phase properties at the particle locations.

chaslv - Advances liquid phase equations.

intpla - Identifies computational cells and PEs associated

with particles.

srips - Evaluates the liquid phase contributions for use in the CFD and PDF equations.

(4) Continues with steps (2) and (3) until the computations are completed over a global time step of dtgl.

(5) Returns control over to other solvers, e.g. CFD and PDF, and also supply them with source terms averaged over dtgl.

4. subroutine dropdis(rhol,flowdum,sr,fld,smd,nofg):

PURPOSE: This routine computes droplet distribution from the following correlation:

$$dn/n = a*((D/D32)**alp)*exp(-b*((D/D32)**bet))*dD/D32$$

where a, b, alp, and bet are constants.

5. subroutine find\_cntr(i,xx,yy,zz):

PURPOSE: This routine computes the x, y, and z locations of the center of the cell, i. It is used in the particle search algorithm.

6. subroutine find\_xyzface(i):

PURPOSE: This routine computes x, y, and z locations of all the face centers of the element, i. It is used in the particle search algorithm.

7. subroutine intpla:

PURPOSE: This routine performs the following functions:

- (1) Particle search - It really amounts to identifying the computational cell where a particle is located. In parallel computing, it also means identifying the corresponding PE associated with the partitioning of the computational domain where a particle is located.
- (2) Implements appropriate boundary conditions if necessary.
- (3) Reassigns the particles based on the parallel implementation strategy employed.

**8. subroutine intplal:**

PURPOSE: This routine interpolates the gas-phase properties at the particle location. In the present case, a simple zeroth order interpolation is employed.

**9. subroutine prnspr:**

PURPOSE: Write standard output from LSPRAY to Fortran unit 1.

**10. subroutine spray\_int\_rerun:**

PURPOSE: This routine has the following functions:

- (1) Provides initial inputs to the spray computations.
- (2) Restarts from previous data if it is a rerun.

**11. subroutine spray\_pdf\_output:**

PURPOSE: This routine writes output data from EUPDF & LSPRAY computations to restart and standard-output files.

**12. subroutine spray\_pdf\_read\_parameters:**

PURPOSE: This routine reads controlling parameters associated with the EUPDF and LSPRAY solvers. Based on the controlling parameters read, it might invoke an initialization routine of the EUPDF solver which is needed in the thermodynamic & transport properties evaluation.

**13. subroutine sprips:**

PURPOSE: This routine computes the source terms arising from liquid phase contribution, of use in both CFD and Monte Carlo PDF solvers.

smlc(i) = liquid-phase contribution of Eqs. 1 and 2 of  
Section III.  
smlmx(i), smlmy(i), smlmz(i) = liquid-phase contribution  
of Eq. 3 of Section III.  
smle(i) = liquid-phase contribution of Eq. 4 of Section III.

**14. subroutine sy(il,iu,bb,dd,aa,cc):**

PURPOSE: Tri-diagonal matrix solver. It is used in the solution for the droplet internal temperature distribution.





## Appendix III

### A Subroutine Listing for the Read Parameters of LSPRAY and EUPDF

```
c
c      subroutine spray_pdf_read_parameters
c
c      include 'dcfslog.i'
c      include 'dcfslog_rw.i'
c
c      -----
c      ---
c
c      PURPOSE: This routine reads controlling parameters associated
c               with the EUPDF and LSPRAY solvers. Based on the controlling
c               parameters read, it might invoke an initialization routine
c               of the EUPDF solver which is needed in the thermodynamic &
c               transport properties evaluation.
c
c      FORM OF CALL: call spray_pdf_read_parameters
c
c
c      ADDITIONAL I/O:
c
c      INPUT: spray_pdf_parameter_input
c
c      OUTPUT: None
c
c      -----
c      ---
c      lspray controls turning on or off spray computations.
c      lspray = .TRUE. - turns on spray computations.
c               = .FLASE. - otherwise.
c
c      ldread controls reading or not from restart files for
c               spray computations.
c      ldread = .TRUE. - restarts from previous runs.
c               = .FLASE. - starts from initial conditions.
c
c      ispray_mod= This variable controls calls to the spray
c                  solver. The spray solver is called once at
c                  every ispray_mod times of CFD iterations.
```

```

c
c ipread = Assigned unit number for the file: liquid_input.
c idread = Assigned unit number for the file: liquid_results.
c idread2= Assigned unit number for the file: liquid_results_ini.
c idwrit = Assigned unit number for the file: liquid_results_new.
c idwrit2= Assigned unit number for the file: liquid_results_ini.
c
c ipdf controls turning on or off Monte Carlo PDF computations.
c ipdf = 0 turns off Monte Carlo PDF computations.
c       = 1 otherwise.
c
c ns serves two functions depending on whether ns has a
c       zero or non-zero value.
c ns = 0 starts the Monte Carlo PDF computations from
c       initial conditions.
c ns = a non-zero number restarts the computations from
c       a previous run. a non-zero number represents the
c       last iteration number of a previous run which is
c       used in the time-averaging scheme utilized in
c       the PDF computations.
c
c ipdf_mod = This variable controls calls to the PDF
c            solver. The PDF solver is called once at
c            every ipdf_mod times of CFD iterations.
c
c ipdf_num = In a given cycle, the pdf solver is advanced over
c            a number of time steps given by ipdf_num.
c
c irea1 = Assigned unit number for the file: pdf_results.
c irea2 = Assigned unit number for the file: pdf_results_ave.
c iwri1 = Assigned unit number for the file: pdf_results.
c iwri2 = Assigned unit number for the file: pdf_results_ave.
c
c -----
c
c       open(unit=85,file='spray_pdf_parameter_input')
c       read(85,*)
c       read(85,*)lspray,ldread,ispray_mod
c       read(85,*)
c       read(85,*)ipread,idread,idwrit,idread2,idwrit2
c       read(85,*)
c       read(85,*)ipdf,ns,ipdf_mod,ipdf_num

```

```

      read(85,*)
      read(85,*)irea1,irea2,iwri1,iwri2
      close(unit=85)
c
c -----
c ---
c
c Routine rctinp of the PDF solver provides initialization
c parameters used in the thermodynamic and transport property
c evaluation as well as in the chemical kinetics scheme.
c
      if(ipdf.eq.1) then
        call rctinp
      endif
c
c -----
c
      RETURN
      END
c

```



## Appendix IV

### A Subroutine Listing for LSPRAY Code Initialization and Restart

```
c
    subroutine spray_int_rerun
    include 'd3dpar.i'

    include 'cfsparms.i'
    include 'cfsnodes.i'

    include 'cfsxyz.i'
    include 'cfsarea.i'
    include 'cfsface.i'

    include 'cfsbc.i'
    include 'cfschar.i'
    include 'cfssym.i'
    include 'cfsadj.i'
    include 'cfstranslate.i'
    include 'cfsedge.i'
    include 'cfsperiodic.i'

    include 'parallel.i'
    include 'cfsmimd.i'

    include 'd3dcom.i'
    include 'd3dinj.i'
    include 'd3dprl.i'

    include 'dcfslog_rw.i'

    dimension fld(20),fldp(20),sr(20),srp(20)
    logical lminj,lmdis,lpinj,lpdis
c
    common/itemplvt/itemplv
c -----
c ---
c
c
c
c
c PURPOSE: This routine has the following functions:
c
```

```

c      (1) Provides initial inputs to the spray computations.
c      (2) Restarts from previous data if it is a rerun.
c
c      REFERENCES:
c
c      (1) M.S. Raju, 'Heat Transfer and Performance Characteristics
c           of a Dual-Ignition Wankel Engine,' Journal of Engines,
c           the 1992 SAE Transactions, Section 3, pp. 466-509.
c
c      (2) M.S. Raju, 'Combined Scalar-Monte-Carlo-PDF/CFD Computations
c           of Spray Flames on Unstructured Grids With Parallel Computing,'
c           AIAA paper 97-2969, the 33rd AIAA/ASME/SAE/ASEE joint propulsion
c           conference, Seattle, WA, July 06-10, 1997.
c
c FORM OF CALL: call spray_int_rerun
c
c ADDITIONAL I/O:
c
c      INPUT: liquid_input, liquid_results_ini, liquid_results.
c
c
c      OUTPUT: None
c
c -----
c
c      itemplv=0
c
c      INTS_DATA_1= 351
c      INTS_DATA_2= 352
c      PACKS_DATA_1= 451
c -----
c ---
c
c Initialization for parallelization.
c
c For elements whose neighboring cells are located on other
c PEs, store appropriate information on inter-processor
c communications. This information will be used in the particle
c search algorithm.
c
c      ip=0

```

```

do iwho= 1, n_neighbor_to
i= neighbor_to(iwho)
do n=1,number_per_processor(1,i)
ip=ip+1
lphi(n) =isend_element(ip)
enddo
n_elem= number_per_processor(1,i)
irc= send_data_i (iul(i),lphi, n_elem, INTS_DATA_1)
enddo

c
inode=nodes
do iwho= 1, n_neighbor_from
i= neighbor_from (iwho)
nitems= number_per_processor(2,i)
irc= recv_data_i (iul(i),lphi, nitems, INTS_DATA_1)
do 594 n=1,nitems
do 593 j=1,nfaces(inter_element(i,n))
if(interface(i,n).eq.j) then
bctype1(inter_element(i,n),j)=1
element=inter_element(i,n)
edge_id=face_to_edge(element,j)
inode=inode+1
edge(edge_id,1)=inode
c1(inter_element(i,n),j)=inode
ipr_fr_id(inode-nodes) =i
ile_fr_id(inode-nodes) =lphi(n)
endif
593 enddo
594 enddo
enddo

c -----
c
c -----
c ---
c wf = molecular weight of fuel.
c elhi = latent heat of vaporization.
c rho1 = density of liquid fuel.
c cpl = specific heat of liquid fuel.
c -----
c
c -----
c ---

```

```

c tboil = boiling temperature of fuel at normal pressure.
c conl  = thermal conductivity of liquid fuel.
c tdrop = initial droplet temperature.
c ugc   = universal gas constant.
c -----
c
c -----
c ---
c dtgl = Global time step. After advancing the spray
c       computations over dtgl, control is returned over
c       to other solvers such as PDF and CFD. However,
c       the allowable time step (=dtml) for advancing
c       the liquid phase equations is usually much smaller
c       than dtgl in case of steady state computations,
c       Convergence could be improved by providing a
c       spray solution based on the average life of the
c       droplets. For this reason the spray source terms
c       supplied to the CFD and PDF solvers are obtained
c       based on an averaging scheme by advancing the
c       liquid phase equations over a number of time steps
c       equaling about dtgl/dtml.
c
c dtml = allowable time step.
c -----
c
c -----
c ---
c The program facilitates fuel injection through the use of a
c single fuel injector. However, multiple fuel injection in a
c steady state calculation could be simulated by simply
c assigning different initial conditions for the spatial
c locations of the droplet groups associated with each one
c of the different holes.
c
c For a polydisperse spray, the program expects inputs
c on the number of droplet groups, droplet locations, and drop
c velocities. But droplet sizes and droplet number can be
c either input directly or could be computed by making use
c of a correlation for the droplet size distribution.
c
c
c

```



```

c lminj = .true. - if fuel from the main injector is turned on.
c      = .false. - otherwise.
c
c lmdis = .true. - invokes a correlation for droplet size distribution.
c      = .false. - otherwise provide inputs on droplet sizes and
c                  droplet numbers.
c
c dtil = time step for main fuel injection.
c
c flowf = fuel flow rate, kgm/s, of main fuel injection. This input
c        is used only when lmdis = .true.
c
c smdm = Sauter mean diameter. This input is used only when
c        lmdis = .true.
c -----
c
c -----
c ---
      write(6,*)' '
      write(6,*)' --- begins writing from subroutine spray_int_rerun of
1spray solver ---'
      write(6,*)' '
      write(1,*)' '
      write(1,*)' --- begins writing from subroutine spray_int_rerun of
1spray solver ---'
      write(1,*)' '
      open(unit=ipread,file='liquid_input')
      read(ipread,*)
      read(ipread,100)wf,elhi,rhol,cpl
      read(ipread,*)
      read(ipread,100)tboil,conl,tdrop,ugc
      read(ipread,*)
      read(ipread,100)dtgl,dtml
      read(ipread,*)
      read(ipread,101)lminj,lmdis,dtil,flowf,smdm
      close(unit=ipread)
c
      if(ipid.eq.1)then
      write(6,102)wf,elhi,rhol,cpl
      write(6,103)tboil,conl,tdrop,ugc
      write(6,104)dtgl,dtml
      write(6,105)lminj,lmdis,dtil,flowf,smdm

```

```

endif
c -----
c
c -----
c ---
      fphi=16.0*atan(1.0)
      afphi=fphi/(180.0*4.0)
c -----
c
c -----
c --- redefine some parameters
c
      cyfs=elhi*wf/ugc
      cpli=cpl
      conl=conl
c -----
c
c -----
c ---
c Initialize parameters of relevance in solving the partial
c differential equation (pde) associated with the internal
c droplet temperature distribution.
c
      tonc=17.0*conl/(cpli*rhol)
      nde=13
      ndem=nde-1
      nde1=nde+2
      ndm=nde1-1
      nde11=nde1+1
      nde2=nde11+1
      dls=1.0/float(nde1-1)
      do 901 i=1,nde1
        stm(i)=float(i-1)*dls
901    continue
      dlsq=1.0/(dls*dls)
      dls=1.0/dls
c -----
c
c -----
c ---
c nr      = number of particles assigned to a given processor.
c nr_total = total number particles in the spray computations.

```

```

c
      nr=0
      nr_total=0
c -----
c
c -----
c ----
c
c begin initialization for main fuel injection.
c
      if(lminj) then
c
c nmih = number of holes in the main fuel injector.
c nmis = number of streams per hole.
c nmip = number of droplet groups in a given stream.
c nos  = total number of groups in a polydisperse
c        spray representing the main fuel injection.
c
      nmih=1
      nmis=1
      nmip=10
      nos=nmih*nmis*nmip
c
c There are two ways to initialize the droplet sizes, sr(i),
c and droplet mass flow rates, fld(i), of a polydisperse
c spray.
c
c (1) simply input the corresponding values.
c (2) Compute from a droplet size distribution function.
c
      if(.not.lmdis) then
c
c fld(i) = mass flow rate of ith droplet group, kgm/s
c
      fld(1)= 0.7618374184E-05
      fld(2)= 0.3031237247E-04
      fld(3)= 0.4020065171E-04
      fld(4)= 0.3439536158E-04
      fld(5)= 0.2397707249E-04
      fld(6)= 0.3062891119E-04
      fld(7)= 0.3528971865E-04
      fld(8)= 0.1766177411E-04

```

```

        fld(9)= 0.2589013457E-04
        fld(10)=0.7142747199E-04
c
c sr(i) = droplet size of the ith droplet group.
c
        sr(1)= 0.4308124971E-05
        sr(2)= 0.9601875718E-05
        sr(3)= 0.1489562419E-04
        sr(4)= 0.2019000021E-04
        sr(5)= 0.2548375051E-04
        sr(6)= 0.3254249896E-04
        sr(7)= 0.4136625284E-04
        sr(8)= 0.5018937372E-04
        sr(9)= 0.6077750004E-04
        sr(10)= 0.7665937301E-04
c
c flowf = total mass flow rate of main fuel injection.
c
        flowf =fld(1)+fld(2)+fld(3)+fld(4)+fld(5)+
>            fld(6)+fld(7)+fld(8)+fld(9)+fld(10)
c
c flowinj = total injected fuel mass per hole per stream.
c
        flowinj=flowf*dtil/float(nmih*nmis)
c
        if(ipid.eq.1)then
        write(6,*)'flowf= ',flowf,' flowinj= ',flowinj
        write(1,*)'flowf= ',flowf,' flowinj= ',flowinj
        endif
c
c convert fld(i) into mass.
c
        fld(1)= dtil*fld(1)
        fld(2)= dtil*fld(2)
        fld(3)= dtil*fld(3)
        fld(4)= dtil*fld(4)
        fld(5)= dtil*fld(5)
        fld(6)= dtil*fld(6)
        fld(7)= dtil*fld(7)
        fld(8)= dtil*fld(8)
        fld(9)= dtil*fld(9)

```

```

        fld(10)= dtil*fld(10)
c
        else
c
c flowinj = total injected fuel mass per hole per stream.
c
        flowinj=flowf*dtil/float(nmih*nmis)
c
        call dropdis(rhol,flowinj,sr,fld,smdm,nmip)
c
        endif
c
c determine droplet number, n_i, of ith group.
c
        andrr1=3.0*fld(1)/(fphi*rhol*(sr(1)**3))
        andrr2=3.0*fld(2)/(fphi*rhol*(sr(2)**3))
        andrr3=3.0*fld(3)/(fphi*rhol*(sr(3)**3))
        andrr4=3.0*fld(4)/(fphi*rhol*(sr(4)**3))
        andrr5=3.0*fld(5)/(fphi*rhol*(sr(5)**3))
        andrr6=3.0*fld(6)/(fphi*rhol*(sr(6)**3))
        andrr7=3.0*fld(7)/(fphi*rhol*(sr(7)**3))
        andrr8=3.0*fld(8)/(fphi*rhol*(sr(8)**3))
        andrr9=3.0*fld(9)/(fphi*rhol*(sr(9)**3))
        andrr10=3.0*fld(10)/(fphi*rhol*(sr(10)**3))
c
c store droplet sizes and droplet numbers in an array form
c for later use.
c
        do 133 iz1=1,nmih
        do 133 iz2=1,nmis
            rdrop(iz1,iz2,1)=sr(1)
            rdrop(iz1,iz2,2)=sr(2)
            rdrop(iz1,iz2,3)=sr(3)
            rdrop(iz1,iz2,4)=sr(4)
            rdrop(iz1,iz2,5)=sr(5)
            rdrop(iz1,iz2,6)=sr(6)
            rdrop(iz1,iz2,7)=sr(7)
            rdrop(iz1,iz2,8)=sr(8)
            rdrop(iz1,iz2,9)=sr(9)
            rdrop(iz1,iz2,10)=sr(10)
c
            ndrrte(iz1,iz2,1)=andrr1

```

```

        ndrrte(iz1,iz2,2)=andrr2
        ndrrte(iz1,iz2,3)=andrr3
        ndrrte(iz1,iz2,4)=andrr4
        ndrrte(iz1,iz2,5)=andrr5
        ndrrte(iz1,iz2,6)=andrr6
        ndrrte(iz1,iz2,7)=andrr7
        ndrrte(iz1,iz2,8)=andrr8
        ndrrte(iz1,iz2,9)=andrr9
        ndrrte(iz1,iz2,10)=andrr10
133      continue
c
        if(ipid.eq.1)then
            print *, ' from main, ndrr= '
            print *,andrr1,andrr2,andrr3,andrr4,
>             andrr5,andrr6,andrr7,andrr8,
>             andrr9,andrr10
        endif
c
c In the present case, the initial particle x location
c is assumed to be the same as the center location
c of the second cell of the computational domain assigned
c to processor one.
c
c compute coordinates of cell 2 on processor one.
c
        if(ipid.eq.1)then
            ijk=2
            call find_cntr(ijk,xctr,yctr,zctr)
            xcu= xctr
            xphi(1) =xctr
            do n=2,np
                rc = send_data_r (iul(n),xphi, 1, PACKS_DATA_1)
            enddo
        endif
        if(ipid.ne.1) then
            rc = recv_data_r (iul(1),xphi, 1, PACKS_DATA_1)
            xcu =xphi(1)
        endif
c
c define x component of initial particle location.
c
        dxloc(1,1,1)= xcu

```

```

dxloc(1,1,2)= xcu
dxloc(1,1,3)= xcu
dxloc(1,1,4)= xcu
dxloc(1,1,5)= xcu
dxloc(1,1,6)= xcu
dxloc(1,1,7)= xcu
dxloc(1,1,8)= xcu
dxloc(1,1,9)= xcu
dxloc(1,1,10)=xcu
c
c define y component of initial particle location.
c
dyloc(1,1,1)= 0.6093000062E-02
dyloc(1,1,2)= 0.5948499776E-02
dyloc(1,1,3)= 0.5214500241E-02
dyloc(1,1,4)= 0.4474000074E-02
dyloc(1,1,5)= 0.4054999910E-02
dyloc(1,1,6)= 0.3895000089E-02
dyloc(1,1,7)= 0.4139999859E-02
dyloc(1,1,8)= 0.5106000230E-02
dyloc(1,1,9)= 0.4997999873E-02
dyloc(1,1,10)=0.4944500048E-02
c
c define z component of initial particle location.
c
dzloc(1,1,1)= 0.0
dzloc(1,1,2)= 0.0
dzloc(1,1,3)= 0.0
dzloc(1,1,4)= 0.0
dzloc(1,1,5)= 0.0
dzloc(1,1,6)= 0.0
dzloc(1,1,7)= 0.0
dzloc(1,1,8)= 0.0
dzloc(1,1,9)= 0.0
dzloc(1,1,10)=0.0
c
c Assign approximate computational cell and processor IDS.
c
do 132 iz1=1,nmih
do 132 iz2=1,nmis
do 132 iz3=1,nmip
ieloc(iz1,iz2,iz3)=3

```

```

        iploc(iz1,iz2,iz3)=1
132    continue
c
c define u component of drop velocity.
c
        uloc(1,1,1) = 28.15850067
        uloc(1,1,2) = 25.18750000
        uloc(1,1,3) = 21.06999969
        uloc(1,1,4) = 17.26049995
        uloc(1,1,5) = 13.75449944
        uloc(1,1,6) = 12.12549973
        uloc(1,1,7) = 11.65199947
        uloc(1,1,8) = 14.19849968
        uloc(1,1,9) = 18.00499916
        uloc(1,1,10)= 3.732000113
c
c define v component of drop velocity.
c
        vloc(1,1,1) = 34.446
        vloc(1,1,2) = 30.130
        vloc(1,1,3) = 22.646
        vloc(1,1,4) = 16.191
        vloc(1,1,5) = 11.856
        vloc(1,1,6) = 10.621
        vloc(1,1,7) = 8.212
        vloc(1,1,8) = 13.201
        vloc(1,1,9) = 11.249
        vloc(1,1,10)= 4.845
c
c define w component of drop velocity.
c
        wloc(1,1,1) = 15.246
        wloc(1,1,2) = 12.511
        wloc(1,1,3) = 10.227
        wloc(1,1,4) = 8.206
        wloc(1,1,5) = 6.760
        wloc(1,1,6) = 5.251
        wloc(1,1,7) = 5.830
        wloc(1,1,8) = 3.972
        wloc(1,1,9) = 5.255
        wloc(1,1,10)= 4.203
c

```



```

c load the above particle attributes into appropriate
c arrays based on the strategy used for parallel
c implementaion.
c
      do 135 iz1=1,nmih
      do 135 iz2=1,nmis
      do 135 iz3=1,nmip
      if(iploc(iz1,iz2,iz3).eq.ipid)then
      nr=nr+1
      xki(nr)=dxloc(iz1,iz2,iz3)
      yki(nr)=dyloc(iz1,iz2,iz3)*(1.35-0.70*rand())
      zki(nr)=dzloc(iz1,iz2,iz3)
      uki(nr)=uloc(iz1,iz2,iz3) *(1.25-0.50*rand())
      vki(nr)=vloc(iz1,iz2,iz3) *(1.25-0.50*rand())
      wki(nr)=wloc(iz1,iz2,iz3) *(1.30-0.60*rand())
      tki(nr)=tdrop
      ski(nr)=rdrop(iz1,iz2,iz3)*rdrop(iz1,iz2,iz3)
      rki(nr)=rdrop(iz1,iz2,iz3)
      sklim(nr)=0.04*rdrop(iz1,iz2,iz3)*rdrop(iz1,iz2,iz3)
      ndrr(nr)=ndrrte(iz1,iz2,iz3)
      isen(nr)=ieloc(iz1,iz2,iz3)
      isep(nr)=iploc(iz1,iz2,iz3)
      ins(nr)=nr
      do i3=1,nde1
      vh(nr,i3)=0.0
      enddo
      vh(nr,nde11)=0.0
      smass=fphi*rhol*(rki(nr)**3)*float(ndrr(nr))/(3.0)
      vh(nr,nde2)=smass
      endif
135   continue
c
      nr_total=nr_total+nos
c
      endif
c
c ---- end of main fuel injecton
c -----
c
c -----
c ----
c t1 =   time associated with dtgl

```

```

c tm1=   time associated with dtml
c tl1=   time associated with dtl
c
      t1 =0.0
      tm1=0.0
      tl1  = 0.0
      if(.not.lminj)tl1  = 1.0e+10
c -----
c
c -----
c ----
c read restart files if ldread = .true.
c
      if(ldread) then
        if(ipid.eq.1) then
          open(unit=idread2,file='liquid_results_ini')
          read(idread2,*)nr_total
          read(idread2,*)dtilte,dtmlte,t1,tl1,tm1
          read(idread2,*)iseed
          close(unit=idread2)
          dphi(1)=dtilte
          dphi(2)=dtmlte
          dphi(3)=t1
          dphi(4)=tl1
          dphi(5)=tm1
          lphi(1)=nr_total
          lphi(2)=iseed
          do n=2,np
            ns_elm=2
            irc= send_data_i (iul(n),lphi, ns_elm, INTS_DATA_2)
            ns_elm=2*5
            rc = send_data_r (iul(n),dphi, ns_elm, PACKS_DATA_1)
          enddo
        endif
        if(ipid.ne.1) then
          ns_elm=2
          irc= recv_data_i (iul(1),lphi, ns_elm, INTS_DATA_2)
          ns_elm=2*5
          rc = recv_data_r (iul(1),dphi, ns_elm, PACKS_DATA_1)
          dtilte  =dphi(1)
          dtmlte  =dphi(2)
          t1      =dphi(3)

```

```

t11      =dphi(4)
tm1      =dphi(5)
nr_total=lphi(1)
iseed    =lphi(2)
endif

```

c

```

write(1,*)' begin outputting records from restart file'
open(unit=idread,file='liquid_results',
> access='direct',recl=136,form='unformatted')
do ip=1,nr_total
  irecord=ip
  read(idread,rec=irecord) ndrr(ip),ins(ip),
1 isen(ip),xki(ip),yki(ip),zki(ip),uki(ip),
2 vki(ip),wki(ip),tki(ip),rki(ip),ski(ip),sklim(ip),
3 (vh(ip,j),j=1,nde+4)
  if(ip.ge.1) then
    write(1,*) ip,ndrr(ip),ins(ip),
1 isen(ip),xki(ip),yki(ip),zki(ip),uki(ip),
2 vki(ip),wki(ip),tki(ip),rki(ip),ski(ip),sklim(ip),
3 (vh(ip,j),j=1,nde+4),irecord
  endif
enddo
close(unit=idread)
write(1,*)' end outputting records from restart file'

```

c

```

nr=0
do ip=1,nr_total
  ispr_el_tno=isen(ip)
  isent=mod(ispr_el_tno,nodes)
  if(isent.eq.0)isent=nodes
  isept=(ispr_el_tno-1)/nodes + 1
  if(ipid.eq.isept)then
    nr=nr+1
    isen(nr)=isent
    isep(nr)=isept
    xki(nr) =xki(ip)
    yki(nr) =yki(ip)
    zki(nr) =zki(ip)
    ski(nr) =ski(ip)
    rki(nr) =rki(ip)
    sklim(nr)=sklim(ip)
    uki(nr) =uki(ip)
  endif
enddo

```

```

vki(nr) =vki(ip)
wki(nr) =wki(ip)
tki(nr) =tki(ip)
ins(nr) =ins(ip)
ndrr(nr) =ndrr(ip)
do jk=1,nde2
vh(nr,jk)=vh(ip,jk)
enddo
endif
enddo
endif

c
c -----
c
c -----
c ---
c

if(ipid.eq.1) then
write(6,*)'nr= ',nr,' nr_total= ',nr_total
write(6,*)'ndrr= ',(ndrr(ip),ip=1,nr)
write(6,*)'nos= ',nos
write(6,*)'tm1= ',tm1,' dtml= ',dtml
write(6,*)'t1= ',t1,' dtgl= ',dtgl
write(6,*)'tl1= ',tl1,' dtil= ',dtil
endif

c -----
write(6,*)' '
write(6,*)' --- ends writing from subroutine spray_int_rerun of
1spray solver ---'
write(6,*)' '
write(1,*)' '
write(1,*)' --- ends writing from subroutine spray_int_rerun of
1spray solver ---'
write(1,*)' '
return
100 format(4e16.10)
101 format(2l2,3e16.10)
102 format(1x,'wf= ',f5.1,' elhi= ',e11.5,
1' rhol= ',f4.0,' cpl= ',f8.3)
103 format(1x,'tboil= ',f5.1,' conl= ',e11.5,
1' tdrop= ',f5.1,' ugc= ',f11.2)
104 format(1x,'dtgl= ',e11.5,' dtml= ',e11.5)

```

```
105  format(1x,'lminj= ',l2,' lmdis= ',l2,  
1' dt1l= ',e11.5,' flowf= ',e11.5,' smdm= ',e11.5)  
end  
c
```



## Appendix V

### An Example LSPRAY Input file

For a description of the variables used in *liquid\_input* file, refer to Appendix IV.

```
wf,elhi,rhol,cpl
0.1002000000E+030.3644438200E+060.6880000000E+030.2249275500E+04
tboil,conl,tdrop,ugc
0.3715000000E+031.0333450000E-010.3140000000E+030.8314900000E+04
dtgl,dtml
0.1500000000E-020.7500000000E-05
lminj,lmdis,dtil,flowf,smdm
T F0.1500000000E-020.3174018348E-030.1200000000E-03
```





## Appendix VI

### A Subroutine Listing for LSPRAY and EUPDF Data Output

```
c
      subroutine spray_pdf_output
c
      include 'cfsparms.i'
      include 'cfsdt.i'
      include 'cfspert.i'
      include 'cfsconv.i'
      include 'cfstime.i'
      include 'cfsmimd.i'

      include 'cfsarea.i'
      include 'cfsnodes.i'
      include 'cfsvars.i'
      include 'cfsprop.i'
      include 'cfsh.i'
c
c Include common blocks associated with spray and PDF computations.
c
      include 'dcfslog.i'
      include 'dcfslog_rw.i'
c
c Include common blocks associated with PDF computations.
c
      include 'p3dpar.i'
      include 'p3dcom.i'
      include 'p3dave.i'
      include 'p3dpro.i'
c
c Include common blocks associated with spray computations.
c
      include 'd3dpar.i'
      include 'd3dcom.i'
      include 'd3dinj.i'
      include 'd3dprl.i'
c
c -----
c ---
c
```

```

c PURPOSE: This routine writes output data from PDF & spray
c           computations on a separate restart and standard
c           output files.
c
c FORM OF CALL: call spray_pdf_output
c
c
c ADDITIONAL I/O:
c
c   INPUTS: None.
c
c   OUTPUTS:
c     liquid_results_new
c     liquid_results_ini
c     spray_pdf_parameter_input
c
c -----
c
c -----
c ---
c
c Write spray restart files.
c
c   if(lspray) then
c     open(unit=idwrit,file='liquid_results_new',
c >    access='direct',recl=136,
c >    form='unformatted')
c     if(ipid.eq.1) then
c       open(unit=idwrit2,file='liquid_results_ini')
c       write(idwrit2,*)nr_total
c       call flush(idwrit2)
c       write(idwrit2,*)dtil,dtml,t1,tl1,tm1
c       call flush(idwrit2)
c       write(idwrit2,*)iseed
c       call flush(idwrit2)
c       close(unit=idwrit2)
c     endif
c
c   INTS_DATA_2=314
c   do n=1,np
c     no_to_ip(n)=nr

```

```

        enddo
        do n=1,np
        if(ipid.ne.n) then
        irc= send_data_i (iul(n),no_to_ip(n), 1, INTS_DATA_2)
        endif
        enddo
        do n=1,np
        if(ipid.ne.n) then
        irc= recv_data_i (iul(n),no_fr_ip(n), 1, INTS_DATA_2)
        endif
        enddo
        no_fr_ip(ipid)=no_to_ip(ipid)
        irecordd=0
        do n=1,ipid-1
        irecordd=irecordd+no_fr_ip(n)
        enddo
c
        do ip=1,nr
        irecord=irecordd+ip
        isent=isen(ip)+(isep(ip)-1)*nodes
        write(idwrit,rec=irecord) ndrr(ip),ins(ip),
1  isent,xki(ip),yki(ip),zki(ip),uki(ip),
2  vki(ip),wki(ip),tki(ip),rki(ip),ski(ip),sklim(ip),
3  (vh(ip,j),j=1,nde+4)
        call flush(idwrit)
        if(ip.ge.1) then
        write(1,*) irecord,ndrr(ip),ins(ip),
1  isent,xki(ip),yki(ip),zki(ip),uki(ip),
2  vki(ip),wki(ip),tki(ip),rki(ip),ski(ip),sklim(ip),
3  (vh(ip,j),j=1,nde+4),nr,nr_total,irecord
        endif
        enddo
        close(unit=idwrit)
        endif
c
c -----
c
c -----
c ---
c
c Update file: spray_pdf_parameter_input.
c Also, write PDF restart files.

```

```

c
c
      if(ipdf.eq.1) then
        if(ipid.eq.1) then
          open(unit=85,file='spray_pdf_parameter_input')
          write(85,*)'lspray ldread ispray_mod'
          write(85,*)lspray,ldread,ispray_mod
          write(85,*)'ipread idread idwrit idread2 idwrit2'
          write(85,*)ipread,idread,idwrit,idread2,idwrit2
          write(85,*)'ipdf ns ipdf_mod ipdf_num'
          write(85,*)ipdf,ns,ipdf_mod,ipdf_num
          write(85,*)'irea1 irea2 iwri1 iwri2'
          write(85,*)irea1,irea2,iwri1,iwri2
          close(unit=85)
        endif
        call outpdf2(ns)
      endif
c
c -----
c
c -----
c ---
c
c Write output of spray computations either to unit
c one or to the screen.
c
      if(lspray) call prnspr
c
      return
      END
c
c

```

## Appendix VII

### A Listing of Geometric Variables Used in LSPRAY and EUPDF

```
c -----
c ---
c
c The spray module expects the following inputs on
c the grid related information:
c
c nodes = total number of the computational elements.
c nedge = total number of faces in the computational domain.
c nfaces(i) = total number of faces of the element, i.
c
c edge(i,1) and edge(i,2) represent the adjacent elements of
c the face, i, if the face happens to be an interface between two
c elements. Otherwise edge(i,1) represents the corresponding
c boundary condition identifier if the face happens to
c represent a computational boundary condition.
c
c face_to_edge(i,j) represents the face ID of the element, i,
c and the face, j.
c
c c1(i,j) provides connectivity map. c1(i,j) = adjacent element
c ID of the element, i, and the face, j, otherwise
c c1(i,j) = boundary condition identifier on any boundary.
c
c vol(i) = volume of the element, i.
c
c areax(i), areay(i), and areaz(i) are the cartesian components
c of the outward pointing area vector of the face, i.
c
c x1(i), y1(i), z1(i) are the cartesian components of the node
c one of the element, i. Similarly, x2(i), y2(i), z2(i)
c are for node 2 and so on.
c
c triangle(i) is .true. if i is a triangular element. Similarly,
c quadrilateral(i), tetrahedron(i), and wedge(i) are logical
c variables representing other type of elements.
c
c axisymmetric is set to .true. for axisymmetric computations
c otherwise it is .false. The axisymmetric computations are
```

c performed by generating 3D elements from a 2D mesh with  
c an arc centered around the z coordinate,  $z=0.0$ . The angle of  
c the arc is defined by the variables, ARC, in radians and THETA0,  
c in degrees.

c

c -----

c

## Appendix VIII

### An Example of the Partial Listings of Code Initiation for Coupling LSPRAY and EUPDF With a Gas Flow Solver

1. The following segment shows how include calls to  
spray\_int\_rerun & pdf\_int\_rerun.

```
c
c -----
c ---
c
c Include common blocks associated with spray and PDF computations.
c
c     include 'dcfslog.i'
c     include 'dcfslog_rw.i'
c
c
c Initialize Monte Carlo PDF computations.
c
c     if(ipdf.eq.1) then
c       call pdf_int_rerun
c     endif
c
c Initialize spray computations.
c
c     IF(1spray) then
c       call spray_int_rerun
c     endif
c
c -----
```

II. The following segment shows how to include calls to DCLR &  
PDF.

```
c
c Include common blocks associated with spray and PDF computations.
c
c     include 'dcfslog.i'
c
c     double precision tbiggas, tendgas, totaltgas
```

```

c -----
c ---
c
c
c Call dclr in order to advance the spray computations
c over a time step of dtgl.
c
      if(lspray.and.mod(iteration,ispray_mod).eq.0) then
        call dclr
      endif
c
c -----
c
c -----
c ---
c
c
c Call pdf in order to advance the PDF computations
c over the next time step.
c
      if(ipdf.eq.1.and.mod(iteration,ipdf_mod).eq.0) then
        do i=1,ipdf_num
          call pdf
        enddo
      endif
c
c -----
c

```

**III. The following segment shows how to include the interphase contributions to the gas phase governing equations.**

```

c -----
c ---
c
c Include common blocks associated with spray and PDF computations.
c
      include 'dcfslog.i'
c
c Include common blocks associated with spray the solver.
c

```



```

        include 'd3dqat.i'
c
c -----
c
c -----
c ---
c
c Include liquid-phase contributions to mass, momentum, species,
c and energy equations.
c
    if(lspray) then
        do i=1,nodes
            sourcem(i)=sourcem(i)+smlc(i)
            sourceu(i)=sourceu(i)+smlmx(i)
            sourcev(i)=sourcev(i)+smlmy(i)
            sourcew(i)=sourcew(i)+smlmz(i)
            sourcef(i)=sourcef(i)+smlc(i)
            sourceh(i)=sourceh(i)+smle(i)
        enddo
    endif
c
c -----

```



## Appendix IX

### An Example Summary of CPU Times Taken By CORSAIR and LSPRAY

Table 2 summarizes the cpu times per cycle taken by CORSAIR and LSPRAY versus the number of processors used on the NASA LeRC LACE cluster. These computations refer to the case of a confined swirl-stabilized spray flame as reported in Ref. 9. The computations were performed on a grid of 2486 quadrilateral elements. It takes approximately about 1000 to 2000 cycles for the computations to reach a converged solution. These results should be considered as preliminary because, as reported in Ref. 9, the parallel performance of the spray computations was found to be reasonable on massively parallel computers like Cray T3D but poor on workstation clusters like LACE. In ref. 9, the results obtained from different decomposition strategies were also summarized. We are in the process of exploring ways to improve upon the parallel performance of LSPRAY in a workstation-cluster environment.

Table 2. Cpu time (sec) per cycle versus number of PEs on LACE Cluster.					
Solver	Characteristic	Number of processors			
		2	4	8	16
CORSAIR	5 steps/cycle	3.55	1.90	1.10	0.60
LSPRAY	100 steps/cycle	0.72	1.00	2.00	6.00

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